

**ΠΑΝΕΛΛΑΔΙΚΕΣ ΕΞΕΤΑΣΕΙΣ Γ' ΤΑΞΗΣ ΗΜΕΡΗΣΙΟΥ ΓΕΝΙΚΟΥ ΛΥΚΕΙΟΥ**

**ΦΥΣΙΚΗ ΠΡΟΣΑΝΑΤΟΛΙΣΜΟΥ (ΝΕΟ ΣΥΣΤΗΜΑ)**

**ΘΕΜΑ Α**

- A1) β      A2) γ      A3) β      A4) δ      A5) Σ - Λ - Σ - Λ - Λ

**ΘΕΜΑ Β**

**B1**

α) σωστό (iii)

β)

$$f_1 = \frac{U}{U + U_s} \cdot f_s = \frac{U}{U + \frac{10}{U}} \cdot f_s \rightarrow f_1 = \frac{10}{11} \cdot f_s$$

$$f_2 = \frac{U}{U - U_s} \cdot f_s = \frac{U}{U - \frac{10}{U}} \cdot f_s \rightarrow f_2 = \frac{10}{9} \cdot f_s$$

$$\frac{f_1}{f_2} = \frac{\frac{10}{11} \cdot f_s}{\frac{10}{9} \cdot f_s} \rightarrow \frac{f_1}{f_2} = \frac{9}{11}$$

**B2**

α) σωστό (i)

β) 
$$U_0 = \omega \cdot A' = \frac{2\pi}{T} 2A \sigma \nu \nu \frac{2\pi \chi}{\lambda} = \frac{2\pi}{T} 2A \sigma \nu \nu \frac{2\pi 9\lambda}{8\lambda} = \frac{2\pi}{T} 2A \sigma \nu \nu \frac{9\pi}{4} = \frac{2\pi}{T} 2A \sigma \nu \nu \frac{\pi}{4} = \frac{2\pi A \sqrt{2}}{T}$$

**B3**

α) σωστό (ii)

β) 
$$\frac{1}{2} \cdot p \cdot u_A^2 = \Lambda$$

$$\frac{1}{2} \cdot p \cdot u_B^2 = \frac{1}{2} \cdot p \cdot 4 \cdot u_A^2 = 4 \cdot \Lambda$$

$$P_A = P_B \rightarrow A_A \cdot U_A = A_B \cdot U_B \rightarrow 2A_B \cdot U_A = A_B \cdot U_B \rightarrow U_B = 2 \cdot U_A$$

$$\Delta P = P_B - P_A = \frac{1}{2} \cdot p \cdot u_B^2 - \frac{1}{2} \cdot p \cdot u_A^2 = 4\Lambda - \Lambda \rightarrow \Delta P = 3\Lambda$$

**ΘΕΜΑ Γ**

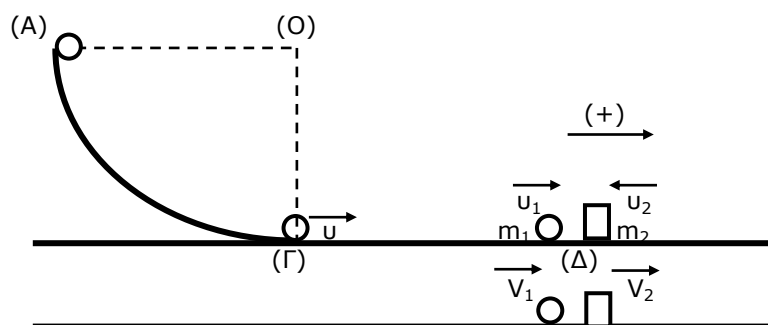
**Γ1**

Α.Δ.Ε. (Α) - (Γ) :

$$m_1 \cdot g \cdot R = \frac{1}{2} \cdot m_1 \cdot v^2 \Rightarrow$$

$$\Rightarrow v = \sqrt{2 \cdot g \cdot R} = \sqrt{2 \cdot 10 \cdot 5} \Rightarrow$$

$$\Rightarrow v = 10 \text{ m/sec}$$



**Γ2**

$$\text{ΑΔΕ(}\Gamma,\Delta\text{)} : \frac{1}{2} \cdot m_1 \cdot u^2 = \frac{1}{2} \cdot m_1 \cdot u_1^2 + \mu \cdot m_1 \cdot g \cdot S \Rightarrow \frac{1}{2} \cdot 100 = \frac{1}{2} \cdot u_1^2 + 0,5 \cdot 10 \cdot 3,6 \Rightarrow$$

$$\Rightarrow 100 = u_1^2 + 36 \Rightarrow u_1^2 = 64 \Rightarrow u_1 = 8 \text{ m/sec}$$

$$V_1 = \frac{m_1 - m_2}{m_1 + m_2} u_1 + \frac{2m_2}{m_1 + m_2} u_2 = \frac{m_1 - 3m_1}{m_1 + 3m_1} \cdot 8 + \frac{2 \cdot 3m_1}{m_1 + 3m_1} (-4) \rightarrow V_1 = -10 \text{ m/sec}$$

$$V_2 = \frac{2m_1}{m_1 + m_2} u_1 + \frac{m_2 - m_1}{m_1 + m_2} u_2 = \frac{2 \cdot m_1}{m_1 + 3m_1} (8) + \frac{3m_1 - m_1}{m_1 + 3m_1} (-4) \rightarrow V_2 = 2 \text{ m/sec}$$

Άρα  $V_1 = 10 \text{ m/sec}$  με κατεύθυνση προς τα αριστερά ,  
και  $V_2 = 2 \text{ m/sec}$  με κατεύθυνση προς τα δεξιά .

**Γ3**

$$\Delta P_2 = P_2^{\tau\epsilon\lambda} - P_2^{\alpha\rho\chi} \rightarrow \Delta P_2 = -m_2 V_2 - m_2 u_2 \rightarrow \Delta P_2 = -18 \text{ kgm/sec}$$

Άρα με μέτρο  $\Delta p_2 = 18 \text{ Kgr} \cdot \text{m/sec}$

Κατεύθυνση προς τα δεξιά.

**Γ4**

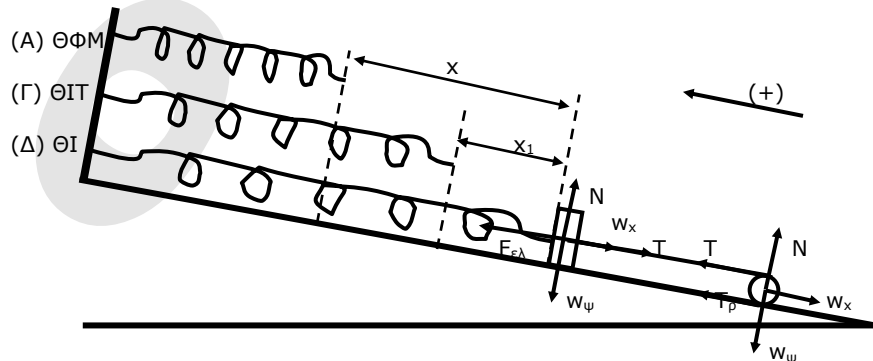
$$\Pi\% = \frac{|K_1^{\alpha\rho\chi} - K_1^{\tau\epsilon\lambda}|}{K_1^{\alpha\rho\chi}} = \frac{|\frac{1}{2} \cdot m_1 \cdot u_1^2 - \frac{1}{2} \cdot m_1 \cdot V_1^2|}{\frac{1}{2} \cdot m_1 \cdot u_1^2} = \frac{|-36|}{64} = 0,56 \rightarrow \Pi\% = 56,25\%$$

**ΘΕΜΑ Δ**

**Δ1**

$$W_{mx} = m g \eta \mu \varphi = 5 \text{ N}$$

$$W_{Mx} = M g \eta \mu \varphi = 10 \text{ N}$$



$$M: \Sigma \tau = 0 \rightarrow TR - T_p R = 0 \rightarrow T = T_p$$

$$\Sigma F_x = 0 \Rightarrow T + T_p = W_{Mx} \Rightarrow 2 \cdot T = 10 \Rightarrow T = 5 \text{ N}$$

$$m: \Sigma Fx = 0 \rightarrow F_{\epsilon\lambda} = W_{mx} + T \rightarrow K \cdot x = 5 + 5 \rightarrow 100x = 10 \rightarrow x = 0,1 \text{ m}$$

**Δ2)**

$$(t=0 \text{ και } x=-A) , \text{ άρα } \varphi_0 = \frac{3\pi}{2} \text{ rad .}$$

$$\Theta.Ι.Τ : \Sigma Fx = 0 \rightarrow F'_{\epsilon\lambda} = W_{mx} = K \cdot x_1 = 5 \rightarrow 100 \cdot x_1 = 5 \rightarrow x_1 = 0,05 \text{ m}$$

$$F_0 = m \cdot \omega^2 \cdot A = 1 \cdot 100 \cdot 0,05 \rightarrow F_0 = 5 \text{ N}$$

$$A = x - x_1 \rightarrow 0,1 - 0,05 \rightarrow A = 0,05 \text{ m}$$

$$D = K = m \cdot \omega^2 \rightarrow 100 = 1 \cdot \omega^2 \rightarrow \omega = 10 \text{ rad/sec}$$

$$\text{και } F = -F_0 \cdot \eta \mu(\omega t + \varphi_0) \rightarrow -5 \cdot \eta \mu(10t + \frac{3\pi}{2}) \text{ (S.I.)}$$

**Δ3)**

$$\Sigma \tau = I \cdot \alpha_{\gamma\omega\nu} \rightarrow T'_p \cdot R = \frac{1}{2} \cdot M \cdot R^2 \alpha_{\gamma\omega\nu} \rightarrow T'_p = \frac{1}{2} \cdot M \cdot \alpha_{cm} \rightarrow T'_p = \alpha_{cm}$$

$$\Sigma F = M \cdot \alpha_{cm} \rightarrow Mg \eta \mu \varphi - T'_p = M \cdot \alpha_{cm} \rightarrow$$

$$\Sigma F_x = m a_{cm} \rightarrow mg \sigma \nu \nu \varphi - T_{\sigma\tau} = m \cdot a_{cm} \rightarrow 10 - a_{cm} = 2 a_{cm} \rightarrow a_{cm} = \frac{10}{3} \frac{m}{s^2}$$

$$a_{cm} = \alpha_{\gamma\omega\nu} \cdot R \rightarrow \alpha_{\gamma\omega\nu} = \frac{100 \text{ rad}}{3 \text{ s}^2}$$

$$N = \frac{\theta}{2\pi} \rightarrow \theta = 24 \text{ rad}$$

$$\theta = \frac{1}{2} \cdot \alpha_{\gamma\omega\nu} \cdot t^2 \rightarrow t^2 = \frac{24 \cdot 6}{100} = 1,2 \text{ sec}$$

$$\omega = \alpha_{\gamma\omega\nu} \cdot t = \frac{100}{3} \cdot 1,2 = \frac{120}{3} = 40 \text{ rad/sec}$$

$$L = I \cdot \omega = \frac{1}{2} \cdot M \cdot R^2 \cdot \omega \rightarrow L = 0,4 \text{ Kgm/s}$$

**Δ4)**

$$\frac{\Delta K}{\Delta t} = \Sigma F \cdot v_1 + \Sigma \tau \cdot \omega_1$$

$$M: \quad \Sigma F = W_{Mx} - T'_p = Mg \eta \mu \varphi - T'_p = \frac{20}{3} \text{ N}$$

$$v_1 = \alpha_{cm} \cdot t = \frac{10}{3} \cdot 3 \Rightarrow v_1 = 10 \text{ m/sec}$$

$$\Sigma \tau = T'_p \cdot R = \frac{10}{3} \cdot 0,1 \rightarrow \Sigma \tau = \frac{1}{3} \text{ N} \cdot \text{m}$$

$$\omega_1 = \alpha_{\gamma\omega\nu} \cdot t \rightarrow \omega_1 = 100 \text{ rad/sec}$$

$$\frac{\Delta K}{\Delta t} = \Sigma F \cdot v_1 + \Sigma \tau \cdot \omega_1$$

$$\frac{\Delta K}{\Delta t} = \frac{20}{3} \cdot 10 + \frac{1}{3} \cdot 100 \rightarrow \frac{\Delta K}{\Delta t} = 100 \text{ J/sec}$$

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